



National  
Qualifications  
2019

**X847/75/01**

**Mathematics  
Paper 1 (Non-calculator)**

FRIDAY, 3 MAY

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**INSTRUCTIONS TO CANDIDATES**

Candidates should enter their surname, forename(s), date of birth, Scottish candidate number and the name and Level of the subject at the top of their first answer sheet.

**Total marks — 50**

Attempt ALL questions.

**You may NOT use a calculator.**

To earn full marks you must show your working in your answers.

State the units for your answer where appropriate.

Write your answers clearly on your answer sheet.

Questions marked with an asterisk differ in some respects from those in the printed paper.

Marks are shown in square brackets at the end of each question or part question.

An OW in the margin indicates a new question.

A separate formulae sheet is provided.

## FORMULAE LIST

The roots of  $ax^2 + bx + c = 0$  are  $x = \frac{-b \pm \sqrt{(b^2 - 4ac)}}{2a}$

Sine rule  $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$

Cosine rule  $a^2 = b^2 + c^2 - 2bc \cos A$  or  $\cos A = \frac{b^2 + c^2 - a^2}{2bc}$

Area of a triangle  $A = \frac{1}{2}ab \sin C$

Volume of a sphere  $V = \frac{4}{3}\pi r^3$

Volume of a cone  $V = \frac{1}{3}\pi r^2 h$

Volume of a pyramid  $V = \frac{1}{3}Ah$

Standard deviation  $s = \sqrt{\frac{\Sigma(x - \bar{x})^2}{n - 1}}$

or  $s = \sqrt{\frac{\Sigma x^2 - \frac{(\Sigma x)^2}{n}}{n - 1}}$ , where  $n$  is the sample size.

Total marks — 50

Attempt ALL questions

1. Given that  $f(x) = 5x^3$ , evaluate  $f(-2)$ . [2 marks]

2. Evaluate  $\frac{3}{8} \times 1\frac{5}{7}$ .

Give your answer in its simplest form. [2 marks]

3. Expand and simplify  $(x + 5)(2x^2 - 7x - 3)$ . [3 marks]

\* 4. Refer to the diagram for Question 4. The diagram shows a sector of a circle, centre C.

The radius of the circle is 30 centimetres.

Calculate the length of the major arc AB.

Take  $\pi = 3 \cdot 14$ . [3 marks]

\* 5. The midday temperatures in Grantford were recorded over a nine day period.

The temperatures, in °C, were

4 7 4 3 6 10 9 5 3

(a) Calculate the median and semi-interquartile range for these temperatures. [3 marks]

Over the same nine day period the midday temperatures in Endoch were also recorded.

The median temperature was 8 °C, and the semi-interquartile range was 1.5 °C.

(b) Make two valid comments comparing the midday temperatures of Grantford and Endoch during this period. [2 marks]

- \* 6. Refer to the diagram for Question 6. It shows a scattergraph.

The fuel consumption of a group of cars is recorded.

The scattergraph shows the relationship between the fuel consumption,  $F$  kilometres per litre, and the engine size,  $E$  litres, of the cars.

A line of best fit has been drawn.

- (a) Find the equation of the line of best fit in terms of  $F$  and  $E$ .  
Give the equation in its simplest form. **[3 marks]**

Amaar's car has an engine size of 1.1 litres.

- (b) Use your equation from part (a) to estimate how many kilometres per litre he should expect to get. **[1 mark]**

- \* 7. The area of a trapezium is given by the formula

$$A = \frac{1}{2}h(x + y).$$

Make  $x$  the subject of the formula. **[3 marks]**

8. John bought 7 bags of cement and 3 bags of gravel.

The total weight of these bags was 215 kilograms.

- (a) Write down an equation to illustrate this information. **[1 mark]**

Shona bought 5 bags of cement and 4 bags of gravel.

The total weight of her bags was 200 kilograms.

- (b) Write down an equation to illustrate this information. **[1 mark]**  
(c) Calculate the weight of one bag of cement and the weight of one bag of gravel.  
**[4 marks]**

- \* 9. Refer to the diagram for Question 9. The graph shows a parabola.  
The maximum turning point has coordinates (4,20) as shown in the diagram.
- (a) Write down the equation of the axis of symmetry of the graph. [1 mark]

The equation of the parabola is of the form  $y = b - (x + a)^2$ .

- (b) State the values of
- (i)  $a$  [1 mark]
- (ii)  $b$ . [1 mark]

- \*10. Refer to the diagram for Question 10. In triangle PQR,  $\vec{PR} = \begin{pmatrix} 6 \\ -4 \end{pmatrix}$  and  $\vec{RQ} = \begin{pmatrix} -1 \\ 8 \end{pmatrix}$ .

- (a) Express  $\vec{PQ}$  in component form. [1 mark]

M is the midpoint of PR.

- (b) Express  $\vec{MQ}$  in component form. [2 marks]

- \*11. Refer to diagrams 1 and 2 for Question 11. Pam is designing a company logo.  
She starts by drawing a regular pentagon ABCDE.  
The vertices of the pentagon lie on the circumference of a circle with centre O, as shown in diagram 1.  
She then adds to the design as shown in diagram 2.  
AF is a diameter of the circle.  
Calculate the size of angle OFB. [3 marks]

12. Express  $\frac{\sqrt{2}}{\sqrt{40}}$  as a fraction with a rational denominator.

Give your answer in its simplest form. [3 marks]

- \*13. Refer to the diagram for Question 13. Part of the graph of  $y = 3\cos(x + 45)^\circ$  is shown in the diagram.

The graph has a minimum turning point at A.

State the coordinates of A. [2 marks]

14. Solve the equation  $\frac{x}{2} - 1 = \frac{3-x}{5}$ . [3 marks]

- \*15. Refer to the diagram for Question 15. A ball is kicked from a clifftop.

The height,  $h$  metres, of the ball relative to the clifftop after  $t$  seconds is given by  $h = 12t - 5t^2$ .

(a) Calculate the height of the ball above the clifftop after 2 seconds. [1 mark]

- \* (b) Refer to the diagram for Question 15(b). The graph represents the height,  $h$  metres, of the ball relative to the clifftop after  $t$  seconds.

The sea is 17 metres below the clifftop.

After how many seconds will the ball hit the sea? [4 marks]

[END OF QUESTION PAPER]