

SQA Databook for HN Physics

For use in Higher National Courses

Publication date: 2016
Publication code: CB7127
ISBN: 978 1 910180 10 5

Published by the Scottish Qualifications Authority
The Optima Building, 58 Robertson Street, Glasgow G2 8DQ
Lowden, 24 Wester Shawfair, Dalkeith, Midlothian EH22 1FD

www.sqa.org.uk

The information in this publication may be reproduced in support of SQA qualifications. If it is reproduced, SQA should be clearly acknowledged as the source. If it is to be used for any other purpose, then written permission must be obtained from SQA. It must not be reproduced for trade or commercial purposes.

© Scottish Qualifications Authority 2016

For an up-to-date list of prices visit the **Publication Sales and Downloads** section of SQA's website.
For further details telephone SQA's Customer Contact Centre on 0845 279 1000.

Contents

Relationships for Physics 1	4
Relationships for Physics 2	5
Waves & Light.	6
Electricity	7
Radiation.	8
Gas & Heat	8
Mechanics	9
Quantum Mechanics.	10
Fundamental Physics Constants	11
DATA SHEET	
Standard Pressure and Temperature	12
Common Physical Quantities	12
Refractive Indices	12
Spectra Lines	13
Properties of Selected Materials.	13
Additional Relationships	14
Electron Arrangements of Elements	15

Relationships for Physics 1

$$v = \frac{s}{t}$$

$$\frac{1}{R_T} = \frac{1}{R_1} + \frac{1}{R_2} + \dots$$

$$v = f\lambda$$

$$\frac{R_1}{R_2} = \frac{R_3}{R_4}$$

$$\tau = \frac{1}{f}$$

$$V_1 = \frac{R_1}{(R_1 + R_2)} \times V_s$$

$$\sin \theta_c = \frac{1}{n}$$

$$P = \frac{E}{t}$$

$$n = \frac{\sin \theta_1}{\sin \theta_2} = \frac{\lambda_1}{\lambda_2} = \frac{v_1}{v_2}$$

$$P = IV = I^2R = \frac{V^2}{R}$$

$$P = \frac{1}{f}$$

$$\frac{N_s}{N_p} = \frac{V_s}{V_p} = \frac{I_p}{I_s}$$

$$A = \frac{N}{t}$$

$$\text{Cost} = \text{unit cost} (\sum Pt)$$

$$D = \frac{E}{m}$$

$$\text{Random uncertainties} = \frac{\text{max value} - \text{min value}}{\text{number of values}}$$

$$H = Dw_r$$

$$\dot{H} = \frac{H}{t}$$

$$V = IR$$

$$\sum E = \sum IR$$

$$R_T = R_1 + R_2 + \dots$$

Relationships for Physics 2

$$v = \frac{s}{t}$$

$$v = f\lambda$$

$$\tau = \frac{1}{f}$$

$$n\lambda = \text{path difference}$$

$$(n + 1/2)\lambda = \text{path difference}$$

$$d \sin \theta = n\lambda$$

$$n = \frac{\sin \theta_1}{\sin \theta_2}$$

$$E = hf$$

$$E = hf - hf_0$$

$$hf = E_1 - E_2$$

$$I = Nhf = N_A hf$$

$$\rho = \frac{m}{V}$$

$$P = \frac{F}{A}$$

$$P = \rho gh$$

$$E_w = Fd$$

$$E_k = \frac{1}{2}mv^2$$

$$E_p = mgh$$

$$\rho_1 A_1 v_1 = \rho_2 A_2 v_2$$

$$P + \rho gh + \frac{1}{2}\rho v^2 = \text{constant}$$

$$Q = Av$$

$$T_{\text{mix}} = \frac{(T_1 m_1 + T_2 m_2)}{(m_1 + m_2)}$$

$$PV = nRT$$

$$PV = N_A k_a T$$

$$Q = kA \left(\frac{\Delta T}{x} \right)$$

$$E_h = cm\Delta T$$

$$E_h = l_v m \quad E_h = l_f m$$

$$H = Ae\sigma T^4$$

Waves & Light

$$v = \frac{s}{t}$$

$$v = f\lambda$$

$$\lambda = \frac{c}{f}$$

$$\tau = \frac{1}{f}$$

$$n\lambda = \text{path difference}$$

$$(n + 1/2)\lambda = \text{path difference}$$

$$d \sin \theta = n\lambda$$

$$n = \frac{\sin \theta_1}{\sin \theta_2} = \frac{\lambda_1}{\lambda_2} = \frac{v_1}{v_2}$$

$$\sin \theta_c = \frac{1}{n}$$

$$n\lambda = n_o + \frac{A}{\lambda^2} \left(\frac{B}{\lambda^2} + \dots \right)$$

$$E = hf$$

$$E = hf - hf_o$$

$$hf = E_1 - E_2$$

$$I = Nh f$$

$$w_2 - w_1 = hf$$

$$P = \frac{1}{f}$$

$$y = A \sin(k\theta - \omega t)$$

$$V_d = \frac{n_d - 1}{n_f - n_c}$$

$$V = \frac{I_{\max} - I_{\min}}{I_{\max} + I_{\min}} \times 100$$

$$\tan \theta = \frac{y}{D}$$

$$\tan \theta = \frac{n_b}{n_a}$$

$$E_p = \int_{\text{aperture}} \cos(kr - \alpha x) dA$$

Electricity

$$V = IR$$

$$B = \frac{\mu_0 I}{2\pi r}$$

$$\sum E = \sum IR$$

$$F = I l B \sin \theta$$

$$R_T = R_1 + R_2 + \dots$$

$$X_c = \frac{V}{I}$$

$$\frac{1}{R_T} = \frac{1}{R_1} + \frac{1}{R_2} + \dots$$

$$X = \frac{1}{2\pi f C}$$

$$\frac{R_1}{R_2} = \frac{R_3}{R_4}$$

$$\varepsilon = -L \frac{dI}{dt}$$

$$V_1 = \frac{R_1}{(R_1 + R_2)} \times V_s$$

$$E = \frac{1}{2} LI^2$$

$$P = \frac{E}{t}$$

$$E = \frac{1}{2} QV = \frac{1}{2} CV^2$$

$$P = IV = I^2 R = \frac{V^2}{R}$$

$$X_L = \frac{V}{I}$$

$$E = \frac{F}{Q}$$

$$X_L = 2\pi f L$$

$$g = \frac{f}{m}$$

$$F = \frac{1}{4\pi\epsilon} \left(\frac{Q_1 Q_2}{r^2} \right)$$

$$E = \frac{Q}{4\pi\epsilon_0 r^2}$$

$$V = \frac{Q}{4\pi\epsilon_0 r}$$

$$E_w = qV$$

Radiation

$$A = \frac{N}{t}$$

$$D = \frac{E}{m}$$

$$H = Dw_r$$

$$\dot{H} = \frac{H}{t}$$

$$N(n) = NAe^{\frac{-En}{kT}}$$

Gas & Heat

$$T_{mix} = \frac{(T_1m_1 + T_2m_2)}{(m_1 + m_2)}$$

$$PV = nRT$$

$$PV = Nk_aT$$

$$E_h = cm\Delta T$$

$$E_h = l_v m \quad E_h = l_f m$$

$$\Delta l = \alpha l_1(T_2 - T_1)$$

$$I = \sigma T^4$$

$$\lambda_{max} = \frac{2.8978 \times 10^{-3}}{T}$$

Mechanics

$$v = \frac{s}{\Delta t}$$

$$a = \frac{(v-u)}{t}$$

$$F = ma$$

$$W = mg$$

$$\omega = \frac{\theta}{t}$$

$$\alpha = \frac{(\omega_2 - \omega_1)}{t}$$

$$s = r\theta$$

$$v = r\alpha$$

$$a = r\alpha$$

$$I = md^2$$

$$I = Mk^2$$

$$IT = I\alpha = Mk^2\alpha$$

$$\rho = \frac{m}{V}$$

$$p = \frac{F}{A}$$

$$p = \rho gh$$

$$E_w = Fd$$

$$E_k = \frac{1}{2}mv^2$$

$$E_p = mgh$$

$$\rho_1 A_1 v_1 = \rho_2 A_2 v_2$$

$$P + \rho gh + \frac{1}{2}\rho v^2 = \text{constant}$$

$$\gamma = \frac{f}{d}$$

$$v = \frac{\pi \rho r^4}{8\eta l}$$

$$\sigma = \frac{F}{A}$$

$$\varepsilon = \frac{\Delta l}{l_0}$$

$$E = \frac{Fl}{Ae}$$

Quantum Mechanics

$$\Delta t = \frac{\Delta t_0}{\sqrt{1 - \frac{v^2}{c^2}}}$$

$$l = l_0 \sqrt{1 - \frac{v^2}{c^2}}$$

$$x' = \frac{x - ut}{\sqrt{1 - \frac{u^2}{c^2}}}$$

$$y' = y; \quad z' = z$$

$$t' = \frac{t - \frac{ux}{c^2}}{\sqrt{1 - \frac{u^2}{c^2}}}$$

$$v' = \frac{v_x - u}{\sqrt{1 - \frac{uv_x}{c^2}}}$$

$$v_x = \frac{v'x + u}{1 + \frac{uv'_x}{c^2}}$$

$$f = \sqrt{\frac{c+u}{c-u}} f_0$$

$$f = \sqrt{\frac{c-u}{c+u}} f_0$$

$$\vec{p} = \frac{m\vec{v}}{\sqrt{1 - \frac{v^2}{c^2}}}$$

$$K = \frac{mc^2}{\sqrt{1 - \frac{v^2}{c^2}}} - mc^2$$

$$\lambda = \frac{h}{p} = \frac{h}{mv}$$

$$E = hf = \frac{hc}{\lambda}$$

$$p = \frac{E}{c} = \frac{hf}{c} = \frac{h}{\lambda}$$

$$\Delta x \Delta p_x \geq \frac{\hbar}{2} \quad (\text{Position and momentum})$$

$$\Delta t \Delta E \geq \frac{\hbar}{2} \quad (\text{energy and time})$$

$$\hbar = \frac{h}{2\pi}$$

$$-\frac{\hbar^2}{2m} \frac{d^2\Psi(x)}{dx^2} + U(x)\Psi(x,t) = i\hbar \frac{\delta\Psi(x,t)}{\delta t}$$

$$\Psi(x,t) = \Psi(x) e^{\frac{-iEt}{\hbar}}$$

$$-\frac{\hbar^2}{2m} \frac{d^2\Psi(x)}{dx^2} + U(x)\Psi(x) = E\Psi(x)$$

$$E_n = \frac{P_n^2}{2m} = \frac{n^2 h^2}{8mL^2} = \frac{n^2 \pi^2 \hbar^2}{2mL^2} \quad (n=1,2,3,\dots)$$

$$\Psi_n(x) = \sqrt{\frac{2}{L}} \sin\left(\frac{n\pi x}{L}\right) \quad (n=1,2,3,\dots)$$

$$E = K + mc^2 = \frac{mc^2}{\sqrt{1 - \frac{v^2}{c^2}}}$$

$$E^2 = (mc^2)^2 + (pc)^2$$

$$E = mc^2$$

$$\int_{-\infty}^{\infty} |\Psi(x)|^2 dx = 1$$

$$T = Ge^{-2kL}$$

Fundamental Physics Constants

<i>Name</i>	<i>Symbol</i>	<i>Value</i>
Gravitational constant	G	$6.67408 \times 10^{-11} \text{ m}^3 \text{ kg}^{-1} \text{ s}^{-2}$
Mass of the earth	M_E	$5.972 \times 10^{24} \text{ kg}$
Radius of the earth	r_E	$6,371 \times 10^3 \text{ m}$
Planck's constant	h	$6.63 \times 10^{-34} \text{ J s}$
Boltzmann's constant	k	$1.38066 \times 10^{-23} \text{ J K}^{-1}$
Stefan – Boltzmann constant	σ	$5.67 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$
Wien's constant	-	$2.90 \times 10^{-3} \text{ m K}$
Avogadro's number	N_A	6.022×10^{23}
Gas constant	R	$8.314510 \text{ J mol}^{-1} \text{ K}^{-1}$
Monatomic Adiabatic index	-	1.67
Mass of electron	m_e	$9.10939 \times 10^{-31} \text{ kg}$
Mass of neutron	m_n	$1.67493 \times 10^{-27} \text{ kg}$
Mass of proton	M_p	$1.67262 \times 10^{-27} \text{ kg}$
Electron volt	eV	$1.603 \times 10^{-19} \text{ J}$
Permittivity of free space	ϵ_0	$8.854 \times 10^{-12} \text{ C}^2 \text{ N m}^{-2}$
	$\frac{1}{4\pi\epsilon_0}$	$8.987 \times 10^9 \text{ N m}^2 \text{ C}^{-2}$
Permeability of free space	μ_0	$4\pi \times 10^{-7} \text{ N A}^{-2}$

DATA SHEET

Standard Pressure and Temperature

<i>Quantity</i>	<i>Symbol</i>	<i>Value</i>
Standard temperature	T	273 K
Standard pressure	P	1.013×10^5 Pa
Molar volume of an ideal gas	-	$\frac{V}{n} = 0.0224 \text{ m}^3 \text{ mol}^{-1}$

Common Physical Quantities

<i>Quantity</i>	<i>Symbol</i>	<i>Value</i>	<i>Quantity</i>	<i>Symbol</i>	<i>Value</i>
Speed of light in vacuum	c	$3.00 \times 10^8 \text{ m s}^{-1}$	Mass of electron	m_e	$9.11 \times 10^{-31} \text{ kg}$
Magnitude of the charge on an electron	e	$1.60 \times 10^{-19} \text{ C}$	Mass of neutron	m_n	$1.675 \times 10^{-27} \text{ kg}$
Gravitational acceleration on Earth	g	9.81 m s^{-2}	Mass of proton	m_p	$1.673 \times 10^{-27} \text{ kg}$
Planck's constant	h	$6.63 \times 10^{-34} \text{ J s}$			

Refractive Indices

The refractive indices refers to sodium light of wavelength 589 nm and to substances at a temperature of 273 K.

<i>Substance</i>	<i>Refractive Index</i>	<i>Substance</i>	<i>Refractive Index</i>
Diamond	2.42	Water	1.33
Crown glass	1.50	Air	1.00

DATA SHEET (continued)

Spectra Lines

<i>Element</i>	<i>Wavelength nm</i>	<i>Colour</i>	<i>Element</i>	<i>Wavelength nm</i>	<i>Colour</i>
Hydrogen	656	Red	Cadmium	644	Red
	486	Blue-green		509	Green
	434	Blue-violet		480	Blue
	410	Violet	Lasers		
	397	Ultraviolet	<i>Element</i>	<i>Wavelength nm</i>	<i>Colour</i>
	389	Ultraviolet	Carbon dioxide	9550	Infrared
Sodium	589	Yellow		10590	Infrared
			Helium-neon	633	Red

Properties Of Selected Materials

<i>Substance</i>	<i>Density kg m⁻³</i>	<i>Melting point K</i>	<i>Boiling point K</i>
Aluminium	2.70×10^3	933	2623
Copper	8.96×10^3	1357	2853
Ice	9.20×10^2	273	
Sea Water	1.02×10^3	264	377
Water	1.00×10^3	273	373
Air	1.29		
Hydrogen	9.00×10^{-2}	14	20

The gas densities refer to a temperature of 273 K and a pressure of 1.01×10^5 Pa

Additional Relationships

Circle

$$\text{circumference} = 2\pi r$$

$$\text{area} = \pi r^2$$

Sphere

$$\text{area} = 4\pi r^2$$

$$\text{volume} = \frac{4}{3}\pi r^3$$

Trigonometry

$$\sin \theta = \frac{\text{opposite}}{\text{hypotenuse}}$$

$$\cos \theta = \frac{\text{adjacent}}{\text{hypotenuse}}$$

$$\tan \theta = \frac{\text{opposite}}{\text{adjacent}}$$

$$\sin^2 \theta + \cos^2 \theta = 1$$

Moment of inertia

point mass

$$I = mr^2$$

rod about centre

$$I = \frac{1}{12}ml^2$$

rod about end

$$I = \frac{1}{3}ml^2$$

disc about centre

$$I = \frac{1}{2}mr^2$$

sphere about centre

$$I = \frac{2}{5}mr^2$$

Table of standard derivatives

$f(x)$	$f'(x)$
$\sin ax$	$a \cos ax$
$\cos ax$	$-a \sin ax$

Table of standard integrals

$f(x)$	$\int f(x)dx$
$\sin ax$	$-\frac{1}{a} \cos ax + C$
$\cos ax$	$\frac{1}{a} \sin ax + C$

Electron Arrangements of Elements

Group 1 Group 2
(1)

1 H	4 Be
Hydrogen 1	(2)
3 Li	2,2 B
2,1 Lithium	Beryllium
11 Na	12 Mg
2,8,1 Sodium	2,8,2 Magnesium
19 K	20 Ca
2,8,8,1 Potassium	2,8,8,2 Calcium
37 Rb	38 Sr
2,8,18,8,1 Rubidium	2,8,18,8,2 Strontium
55 Cs	56 Ba
2,8,18,18,8,1 Caesium	2,8,18,18,8,2 Barium
87 Fr	88 Ra
2,8,18,32,18,8,1 Francium	2,8,18,32,18,8,2 Radium

Key

Atomic number Symbol Electron arrangement Name

Transition Elements

(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)
21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn
Scandium	Titanium	Vanadium	Chromium	Manganese	Iron	Cobalt	Nickel	Copper	Zinc
39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd
Yttrium	Zirconium	Niobium	Molybdenum	Technetium	Ruthenium	Rhodium	Palladium	Silver	Cadmium
57 La	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg
Lanthanum	Hafnium	Tantalum	Tungsten	Rhenium	Osmium	Iridium	Platinum	Gold	Mercury
89 Ac	104 Rf	105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Ds	111 Rg	112 Cn
Actinium	Rutherfordium	Dubnium	Seaborgium	Bohrium	Hassium	Meitnerium	Darmstadtium	Oganesson	Copernicium

Group 3 Group 4 Group 5 Group 6 Group 7 Group 0
(18)

(13)	(14)	(15)	(16)	(17)	(18)
5 B	6 C	7 N	8 O	9 F	10 Ne
2,3 Boron	2,4 Carbon	2,5 Nitrogen	2,6 Oxygen	2,7 Fluorine	2,8 Neon
13 Al	14 Si	15 P	16 S	17 Cl	18 Ar
2,8,3 Aluminium	2,8,4 Silicon	2,8,5 Phosphorus	2,8,6 Sulfur	2,8,7 Chlorine	2,8,8 Argon
31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr
2,8,18,3 Gallium	2,8,18,4 Germanium	2,8,18,5 Arsenic	2,8,18,6 Selenium	2,8,18,7 Bromine	2,8,18,8 Krypton
49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe
2,8,18,18,3 Indium	2,8,18,18,4 Tin	2,8,18,18,5 Antimony	2,8,18,18,6 Tellurium	2,8,18,18,7 Iodine	2,8,18,18,8 Xenon
81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn
2,8,18,32,18,3 Thallium	2,8,18,32,18,4 Lead	2,8,18,32,18,5 Bismuth	2,8,18,32,18,6 Polonium	2,8,18,32,18,7 Astatine	2,8,18,32,18,8 Radon

Lanthanides

57 La	58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu
Lanthanum	Cerium	Praseodymium	Neodymium	Promethium	Samarium	Europium	Gadolinium	Terbium	Dysprosium	Holmium	Erbium	Thulium	Ytterbium	Lutetium
2,8,18,18,9,2	2,8,18,20,8,2	2,8,18,21,8,2	2,8,18,22,8,2	2,8,18,23,8,2	2,8,18,24,8,2	2,8,18,25,8,2	2,8,18,25,9,2	2,8,18,27,8,2	2,8,18,28,8,2	2,8,18,29,8,2	2,8,18,30,8,2	2,8,18,31,8,2	2,8,18,32,8,2	2,8,18,32,9,2
89 Ac	90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr
Actinium	Thorium	Protactinium	Uranium	Neptunium	Plutonium	Americium	Curium	Berkelium	Californium	Einsteinium	Fermium	Mendelevium	Nobelium	Lawrencium

Actinides